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METHOD

OF

Ascertaining the Latitude

IN THE

NORTHERN HEMISPHERE,

BY A

SINGLE ALTITUDE

OF THE

POLAR STAR,

AT ANY TIME;

WITH TABLES

COMPUTED FOR THAT PURPOSE.

By JOHN STEVENS, *R*

In the Service of the East India Company.

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Ascertaining the Latitudes

IN THE

NORTHERN HEMISPHERE

BY

SYDNEY A. MITCHELL

OF THE

POLAR STAR

AND THE

WITH TABLES

COMPILED FOR THE NAVY

BY JOHN STURGES

OF THE ROYAL NAVAL OBSERVATORY

LONDON

Printed by W. BARNARD, at the Office of the Admiralty, Whitehall, and by J. H. COOKE, at the Office of the Hydrographic Office, Admiralty, Whitehall.

1844

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TO
THE HONOURABLE
THE
COURT OF DIRECTORS
OF THE
UNITED COMPANY OF MERCHANTS
OF ENGLAND
TRADING TO THE EAST INDIES,
THIS
METHOD OF ASCERTAINING THE LATITUDE
IN THE NORTHERN HEMISPHERE,
IS, WITH THE GREATEST RESPECT,
DEDICATED
BY THEIR MOST OBEDIENT
HUMBLE SERVANT,
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AS cloudy or hazy Weather, and fogs, very frequently prevent taking Observations of the Sun or Stars when they are upon the Meridian, the following method of ascertaining the Latitude is offered; as it will answer at any time of the night in the Northern Hemisphere, if there should be an interval of clear Weather; and, it is hoped, it will be found scarcely more difficult than that by a Meridian Altitude.

The little trouble that attends it will be compensated by the advantages of an additional method of acquiring the Latitude; advantages which need not be pointed out to Navigators.

The only requisites in this method, are, an Altitude of the Polar Star, and the *apparent* Time. †

When it is said that this method is nearly as easy as that which is most commonly used, the time is supposed to be nearly correct; but as this is not always the case, it will be proper to state, what the error of Latitude arising from an error in the time, may amount to.

If the time should be twenty minutes wrong, when the star is upon the meridian, both above and below the Pole, the error will be scarce any thing, and can never at its greatest distance from the meridian, exceed nine miles and a quarter.

It is generally allowed, that a pretty good Observer may, with a Hadley's Quadrant, take the Altitude of a Star, within about four minutes of the truth, when the horizon of the Sea is tolerably clear.* If a set of Altitudes of a proper Star for correcting the watch, be taken nearly at the same time, with the Altitude of the

† To find the Latitude by the Altitude of any other Star, taken when it is not upon the Meridian, requires a much longer process, as well as an exactness of time, not necessary by an Altitude of the Polar Star; any *probable* error in the time having little effect upon the Latitude so found.

* This error, if it be so great, will be principally owing to the Horizon not being perfectly defined.

Polar Star, the amount of the errors resulting from taking the altitude of the Polar Star, in the time deduced from the Altitude of the other Star, in these Tables, and in the use of them, will not exceed 5 miles in the Latitude; in the present improved state of Instruments and their use, the error can scarcely ever be so much. † Should the Latitude have been obtained from a Meridian Altitude of a Star to the Southward of the Observer, if an Altitude of the Polar Star be immediately taken, and the Latitude ascertained by this method, using the Right Ascension of the Star observed to the Southward, increased by the time it has passed the Meridian, for the Right Ascension of the Mid-heaven, the mean of the Latitudes found by both Stars, will be nearly one-half nearer the truth, than that found by either of them separately; as the errors of observing, as far as they arise from any defect of the Horizon, will be likely to correct each other.

The Principles, Description, and Use of the Tables.

The Polar Star is supposed to be in $88^{\circ} 15'$ North Declination, which is $1^{\circ} 45'$ from the North Pole; now it will be evident, that the Polar Star will describe a circle round the Pole, the Radius of which will be equal to $1^{\circ} 45'$, and that its apparent motion round the Pole will be regular; its greatest elevation above the Pole, or depression below it, must be $1^{\circ} 45'$, equal to its distance from the Pole.

As all celestial Objects are at their greatest Altitude on the Meridian, when the right Ascension of the Mid-heaven or Meridian is the same with that of the Star, the Star must be at its greatest Altitude, or $1^{\circ} 45'$ above the Pole.

The Polar Star's Right Ascension is supposed to be $52^{\circ} 30'$, therefore when the Right Ascension of the Mid-heaven is $52^{\circ} 30'$ the Star will be upon the Meridian.

If the Observer be at the Equator, the Pole will be in the Horizon, the Star's greatest Altitude will be $1^{\circ} 45'$ at $52^{\circ} 30'$ Right Ascension of the Mid-heaven; at

† If Altitudes of a Star on each side of the Meridian, be taken for finding the time, it will *probably* reduce the error of time one half.

6° 52' 30" it will be in the Horizon; at 12° 52' 30" it will be at its greatest depression below the Horizon 1° 45'; and at 18° 52' 30" it will again be in the Horizon, or have no Altitude. Now as its motion is regular, it is only necessary to compute for one Quarter of its Orbit round the Pole, as it will be the same in each quarter. This at first was done by means of Mr. Garrard's Traverse Tables, using 1° 45' equal to 105' for the Hypotenuse, and the distance of the Star from the Meridian, which is equal to the Right Ascension of the Mid-heaven diminished by 52' 30", for one of the Angles, by which means the Altitude was found true to Minutes and to five Decimal places, using his radical Tables; but as this method would be true only in Plane Trigonometry, every altitude was computed to the Right Ascension of the Mid-heaven down the first Column, Table 1. by the following rule:—To the Logarithm of the natural versed sine of the difference between the Right Ascension of the Star and that of the Mid-heaven, expressed in degrees, minutes, and seconds, add the Logarithmic co-sine of the Star's Declination; find the natural number answering to the sum (rejecting 10 in the index), which added to the natural versed sine of the Meridional co-Altitude of the Star, will give the co-versed sine of the true altitude.

When the Pole is elevated, the Star will always (except when upon the Meridian, either above or below the Pole) be lower than shewn by the correction in Table 1. when applied to the Elevation of the Pole, with a contrary sign to that in the Tables, and more so, the higher the Latitude. Table 2. contains what that difference is at each of the Latitudes specified at the top, and at the Right Ascension of the Mid-heaven, expressed at the side, and was computed by the following Rule. To the Logarithm of the natural versed sine of the Star's Meridian Distance, in degrees, minutes, and seconds, add the Logarithmic Co-sines of the Latitude at the top, and of the Star's Declination; find the natural number answering to the above sum (rejecting
Tens

Tens in the Index), which being added to the natural versed sine of the star's Meridional co-Altitude above the Pole, will give the true Altitude; now the difference between this altitude, decreased by the Latitude used in the operation, and the correction in Table 1. for the same Right Ascension of the Mid-heaven, is the corresponding correction in Table 2. for each of the Latitudes at the top of the Columns. Table 2. to minutes and seconds, is the immediate result of this comparison, and the one to minutes and tenths, is found by reducing the seconds to decimals of a minute.

Table 1. has five columns; the middle column contains the difference between the Altitude of the Pole and the Polar Star; the other four columns contain the Right Ascension of the Mid-heaven, to every 10 minutes, within two hours of the Star's being upon the Meridian, both above and below the Pole, and to every 5 minutes for the rest of the 24 hours; the correction of Altitude is to be *subtracted* when the Right Ascension of the Mid-heaven is found in one of the two columns to the left, and to be *added* when it is found in one of the two columns to the right, as directed in the columns of Right Ascension of the Mid-heaven. For example: when the Right Ascension of the Mid-heaven is $4^h 20'$, the corresponding correction $1^{\circ} 4', 8$ is to be subtracted from the observed Altitude of the Polar Star, to find the elevation of the Pole nearly. Or suppose the Right Ascension of the Mid-heaven to be $18^h 26' 40''$, then the corresponding correction $9' 32''$ is to be added to the observed Altitude, and it will give the elevation of the Pole nearly.

Table 2. is a Table of corrections to be added to the Latitude as found by the assistance of Table 1.

It consists of 13 columns, the one to the right and the one to the left containing the Right Ascension of the Mid-heaven, and the other 11 columns contain corrections for the Latitudes specified at the top of the columns. It is to be entered with the Right Ascension

or

of the Mid-heaven in one of the side columns, and the Latitude found by Table 1. at the Top; and the corresponding correction added to the Latitude first found, will give the true Latitude. For example: in $4^h 20'$ Right Ascension of the Mid-heaven, the Altitude of the Polar Star was observed to be $51^\circ 3'$, and the correction from Table 1. being applied to it, gives $49^\circ 58.2$ for the first found Latitude; with this enter Table 2. at the top, and the Right Ascension of the Mid-heaven $4^h 20'$ at the side, and the correction is 1.2 , which added to Latitude, $49^\circ 58.2$, will give $49^\circ 59.4$ the true Latitude. Or suppose the Right Ascension of the Mid-heaven to be $18^h 26' 40''$, and the Altitude observed to be $52^\circ 37' 45''$, the correction from Table 1. which is $9' 32''$, being added to the Altitude, will give $52^\circ 47' 17''$, which will be the Latitude near the truth. Enter Table 2. with the Right Ascension of the Mid-heaven, and Latitude $52^\circ 47'$ at the top, and the corresponding correction taken by proportion, which will always be near enough, will be $2' 5''$, which being added to the Latitude first found, will give $52^\circ 49' 22''$, the true Latitude. †

† It is to be observed, that the argument at the top of the columns is the true Latitude, therefore a small error will arise from taking the Latitude found by Table 1. but this may always be obviated by going through the operation again, with the Latitude last found.

To find the Latitude by these Tables.

With the time, find the Right Ascension of the Mid-heaven as follows: To the Sun's Right Ascension, add the time from the last noon, the sum (rejecting 24 hours if it exceed that sum) will be the right Ascension of the Mid-heaven or Meridian.

Let an Altitude of the Polar Star be taken, and the time noted by a watch; correct the Altitude for Refraction (and dip of the Horizon if the Observation be made with the Horizon of the Sea.)

Apply the error of the watch to the time noted, if there be any error, and find the Right Ascension of the Mid-heaven as above, with which enter Table 1. and there will be found a correction to be *added* to or *subtracted* from the Altitude, as directed in the column of Right Ascension of the Mid-heaven; this will give the Latitude near the truth.

Enter Table 2. with the Latitude thus found at the top, and the Right Ascension of the Mid-heaven at the side; the corresponding correction *added* to the Latitude found as above, will give the true Latitude.

It is to be premised, that in the following examples, Nautical time is used; that is to say, Sept. 10th, 1798, at $10^h 5' 34''$ is $10^h 5' 34''$ after noon on the 9th.

Examples.

I. September 10th, 1798, at $10^h 5' 34''$ the Altitude of the Polar Star was observed to be $26^\circ 46'$ in Longitude $38^\circ 20'$ west, the height of the eye being 20 feet above the level of the Sea.

Time	$10^h 5' 34''$	Altitude	$26^\circ 46'$
Sun's Right Ascension for noon	} 11 12 5	Refraction	— 1.8
Correction for Longitude $38^\circ 20' W.$ and for $10^h 6'$ Table XXIII. requisite Tables.		Dip of the Horizon	— 4.3
	+ 1 54	True Altitude	26 39.9
		Correction Table 1.	— 1 2.9
		Latitude near the truth	25 37
Right Ascension of Mid-heaven	} 21 19 33	Correction Table 2.	+ .5
		True Latitude	25 37.5 N

II. September

II. September 21st, 1798, in Longitude $37^{\circ} 40' W.$ at $3^h 40'$ in the morning, the Latitude was observed by the Meridian Altitude of Jupiter to be $37^{\circ} 47' 30'' N.$ about 1 minute afterwards, the Altitude of the Polar Star was observed to be $39^{\circ} 9' 30''$, the height of the eye being 19 feet above the level of the Sea.

Time	$15^h 41' 0''$	Altitude	$39^{\circ} 9' 30''$
Sun's Right Ascension at noon	$11 51 37$	Refraction	$- 1 10$
Correction for $15^h 41'$ and $37^{\circ} 40' W.$	$+ 2 44$	Dip of the Horizon	$- 4 10$
Right Ascension of Mid-heaven	$3 35 21$	True Altitude	$39 4 10$
		Correction Table 1.	$-1 19 35$
		Latitude near the truth	$37 44 35$
		Correction Table 2.	$+ 33$
		Latitude by the Polar Star	$37 45 8 N$
		Latitude by Jupiter	$37 47 30 N$
		Mean Latitude	$37 46 19 N$

III. September 23d, 1798, in Longitude $34^{\circ} 19' W.$ the Latitude was observed to be $39^{\circ} 51' N.$ by a Meridian Altitude of Rigel, at the same time, the Altitude of the Polar Star was observed by another person to be $40^{\circ} 43'$, the height of the Observer's eye being 19 feet above the level of the Sea.

Right Ascension of Rigel, which is the same with that of the Mid-heaven	$5^h 4' 52''$	Altitude observed	$40^{\circ} 43'$
		Refraction	$- 1,1$
		Dip of the Horizon	$- 4,2$
		True Altitude	$40 37,7$
		Correction Table 1.	$- 47,5$
In this instance, the Latitudes agree near enough, without any correction.		Latitude near the truth	$39 50,2 N$
		Correction Table 2.	$+ 1,1$
		True Latitude	$39 51,3 N$

IV. December 31st, 1799, at Cambridge, at $5^h 44' 20''$ the Altitude of the Polar Star was observed to be $53^{\circ} 57' 45''$;

Sun's Right Ascension at noon	$18^h 38' 46''$	Altitude	$53^{\circ} 57' 45''$
Correction for $5^h 44'$	$+ 1 3$	Refraction	$- 41$
Time	$5 44 20$	True Altitude	$53 57 4$
Right Ascension of the Mid-heaven	$24 9$	Correction Table 1.	$-1 44 12$
		Latitude near the truth	$52 12 52 N$
		Correction Table 2.	$+ 2$
		True Latitude	$52 12 54 N$

When there is so much uncertainty in the time as to make it necessary, or adviseable, to take Altitudes of a celestial object for ascertaining it, the time may be found from them by either of the methods in the requisite Tables, or by any of those in Mr. Mackay's valuable Treatise on the Theory and Practice of finding the Longitude. Mr Mackay's method by the rising or setting of a celestial object, may be particularly useful for this purpose.

TABLE 1.

H	52½	H	52½	"	H	52½	H	52½
1.	0	1.	45	1.	45	0	12.	52½
1.	10	1.	35	1.	44	57	13.	0
1.	20	1.	25	1.	44	42	13.	10
1.	30	1.	15	1.	44	15	13.	20
1.	40	1.	5	1.	43	30	13.	30
1.	50	23.	55	1.	42	45	13.	40
2.	0	23.	45	1.	41	43	13.	50
2.	10	23.	35	1.	40	29	14.	0
2.	20	23.	25	1.	39	3	14.	10
2.	30	23.	15	1.	37	26	14.	20
2.	40	23.	5	1.	35	38	14.	30
2.	50	22.	55	1.	33	39	14.	40
3.	0	22.	45	1.	31	30	14.	50
3.	5	22.	40	1.	29	10	15.	0
3.	10	22.	35	1.	27	56	15.	5
3.	15	22.	30	1.	26	39	15.	10
3.	20	22.	25	1.	25	21	15.	15
3.	25	22.	20	1.	23	59	15.	20
3.	30	22.	15	1.	22	36	15.	25
3.	35	22.	10	1.	21	10	15.	30
3.	40	22.	5	1.	19	41	15.	35
3.	45	22.	0	1.	18	11	15.	40
3.	50	21.	55	1.	16	38	15.	45
3.	55	21.	50	1.	15	3	15.	50
4.	0	21.	45	1.	13	26	15.	55
4.	5	21.	40	1.	11	46	16.	0
4.	10	21.	35	1.	10	5	16.	5
4.	15	21.	30	1.	8	22	16.	10
4.	20	21.	25	1.	6	36	16.	15
4.	25	21.	20	1.	4	49	16.	20
4.	30	21.	15	1.	3	0	16.	25
4.	35	21.	10	1.	1	9	16.	30
4.	40	21.	5		59	17	16.	35
4.	45	21.	0		57	22	16.	40
4.	50	20.	55		55	27	16.	45
4.	55	20.	50		53	29	16.	50
5.	0	20.	45		51	30	16.	55
5.	5	20.	40		49	30	17.	0
5.	10	20.	35		47	28	17.	5
5.	15	20.	30		45	24	17.	10
5.	20	20.	25		43	20	17.	15
5.	25	20.	20		41	14	17.	20
5.	30	20.	15		39	7	17.	25
5.	35	20.	10		36	59	17.	30
5.	40	20.	5		34	50	17.	35
5.	45	20.	0		32	40	17.	40
5.	50	19.	55		30	29	17.	45
5.	55	19.	50		28	17	17.	50
6.	0	19.	45		26	4	17.	55
6.	5	19.	40		23	50	18.	0
6.	10	19.	35		21	36	18.	5
6.	15	19.	30		19	21	18.	10
6.	20	19.	25		17	6	18.	15
6.	25	19.	20		14	50	18.	20
6.	30	19.	15		12	34	18.	25
6.	35	19.	10		10	17	18.	30
6.	40	19.	5		8	1	18.	35
6.	45	19.	0		5	43	18.	40
6.	50	18.	55		3	26	18.	45
6.	52½	18.	52½		1	9	18.	50
						0	18.	52½

Right Ascension of the Mid-heaven, the correction of Altitude to be subtracted.

Correction of Altitude.

Right Ascension of the Mid-heaven, the correction of Altitude to be added.

Enter
and in the
the Obser-
sion. T
Enter
Mid-hea-
above, v

RA of MH

75

70

65

60

55

50

45

40

30

20

10

RA of MH

RA of MH	10	20	30	40	45	50	55	60	65	70	75	RA of MH
H 52½	0	0	0	0	0	0	0	0	0	0	0	H 52½
1. 30	1	1	1	2	3	3	4	5	6	7	11	15
2. 0	2	3	5	7	9	10	12	15	19	25	34	23. 45
2. 30	3	6	9	14	16	20	24	29	37	49	58	23. 15
3. 0	5	10	16	23	28	33	40	49	1. 28	1. 19	1. 51	22. 45
3. 30	7	15	23	33	40	48	58	1. 10	1. 55	2. 29	3. 26	22. 15
4. 0	9	19	30	44	52	1. 2	1. 15	1. 32	2. 13	2. 52	3. 58	21. 45
4. 20	10	22	35	51	1. 8	1. 12	1. 27	1. 47	2. 30	3. 14	4. 27	21. 25
4. 40	12	24	39	57	1. 16	1. 22	1. 38	2. 0	2. 46	3. 34	4. 55	20. 45
5. 0	14	27	44	1. 4	1. 22	1. 31	1. 50	2. 13	2. 59	3. 51	5. 17	20. 25
5. 20	15	30	47	1. 9	1. 28	1. 38	1. 58	2. 24	3. 10	4. 5	5. 36	20. 5
5. 40	16	32	51	1. 14	1. 32	1. 45	2. 11	2. 33	3. 18	4. 15	5. 48	19. 45
6. 0	16	33	53	1. 17	1. 34	1. 49	2. 15	2. 44	3. 26	4. 22	5. 57	19. 25
6. 20	16	34	54	1. 19	1. 36	1. 54	2. 17	2. 46	3. 28	4. 24	5. 59	19. 5
6. 40	17	35	55	1. 20	1. 36	1. 54	2. 17	2. 46	3. 28	4. 24	5. 57	18. 45
7. 0	17	35	56	1. 20	1. 36	1. 54	2. 17	2. 46	3. 28	4. 24	5. 57	18. 25
7. 20	17	35	55	1. 19	1. 34	1. 53	2. 15	2. 43	3. 25	4. 18	5. 53	18. 5
7. 40	16	34	53	1. 17	1. 32	1. 49	2. 10	2. 38	3. 15	4. 9	5. 35	17. 45
8. 0	15	32	50	1. 13	1. 27	1. 43	2. 4	2. 30	3. 5	3. 56	5. 17	17. 25
8. 20	14	30	47	1. 9	1. 22	1. 37	1. 56	2. 21	2. 53	3. 40	4. 56	17. 5
8. 40	13	27	43	1. 3	1. 15	1. 30	1. 47	2. 9	2. 39	3. 22	4. 31	16. 45
9. 0	12	25	39	57	1. 8	1. 21	1. 37	1. 56	2. 23	3. 2	4. 3	16. 25
9. 20	11	22	34	51	1. 0	1. 12	1. 26	1. 43	2. 7	2. 41	3. 35	16. 5
9. 40	9	19	30	44	54	1. 2	1. 14	1. 29	1. 49	2. 19	3. 3	15. 45
10. 0	8	16	26	37	44	1. 2	1. 2	1. 15	1. 32	1. 56	2. 35	15. 25
10. 20	5	12	18	27	31	52	45	54	1. 6	1. 24	2. 51	15. 5
10. 30	4	11	17	27	30	37	27	32	1. 40	1. 51	1. 7	14. 40
11. 5	4	7	12	17	20	23	15	17	21	27	35	14. 10
11. 35	2	4	6	9	10	12	6	10	8	10	14	13. 40
12. 5	1	2	3	4	4	5	0	7	0	0	0	12. 52½

R U L E.

Enter Table 1. with the Right Ascension of the Mid-heaven, in one of the side columns, and in the middle column will be found a Correction to be *added to*, or *subtracted from*, the Observed Altitude (corrected for Refraction,) as directed in the column of Right Ascension. This will give the Latitude near the truth.

Enter Table 2. with the Latitude thus found, at the top, and the Right Ascension of the Mid-heaven at the side; the corresponding Correction *added to* the Latitude found as above, will give the true Latitude.

TABLE 1.

H	H	o	H	H
52½	52½	1. 45,0	12. 52½	12. 52½
1. 0	45	1. 44,9	13. 0	12. 45
1. 10	35	1. 44,7	13. 10	12. 35
1. 20	25	1. 44,2	13. 20	12. 25
1. 30	15	1. 43,6	13. 30	12. 15
1. 40	5	1. 42,8	13. 40	12. 5
1. 50	23. 55	1. 41,7	13. 50	11. 55
2. 0	23. 45	1. 40,5	14. 0	11. 45
2. 10	23. 35	1. 39,1	14. 10	11. 35
2. 20	23. 25	1. 37,4	14. 20	11. 25
2. 30	23. 15	1. 35,6	14. 30	11. 15
2. 40	23. 5	1. 33,7	14. 40	11. 5
2. 50	22. 55	1. 31,5	14. 50	10. 55
3. 0	22. 45	1. 29,2	15. 0	10. 45
3. 5	22. 40	1. 27,9	15. 5	10. 40
3. 10	22. 35	1. 26,7	15. 10	10. 35
3. 15	22. 30	1. 25,3	15. 15	10. 30
3. 20	22. 25	1. 24,0	15. 20	10. 25
3. 25	22. 20	1. 22,6	15. 25	10. 20
3. 30	22. 15	1. 21,2	15. 30	10. 15
3. 35	22. 10	1. 19,7	15. 35	10. 10
3. 40	22. 5	1. 18,2	15. 40	10. 5
3. 45	22. 0	1. 16,6	15. 45	10. 0
3. 50	21. 55	1. 15,1	15. 50	9. 55
4. 0	21. 50	1. 13,4	15. 55	9. 50
4. 5	21. 45	1. 11,8	16. 0	9. 45
4. 10	21. 40	1. 10,1	16. 5	9. 40
4. 15	21. 35	1. 8,4	16. 10	9. 35
4. 20	21. 30	1. 6,6	16. 15	9. 30
4. 25	21. 25	1. 4,8	16. 20	9. 25
4. 30	21. 15	1. 3,0	16. 25	9. 20
4. 35	21. 10	1. 1,2	16. 30	9. 15
4. 40	21. 5	59,3	16. 35	9. 10
4. 45	21. 0	57,4	16. 40	9. 5
4. 50	20. 55	55,4	16. 45	9. 0
4. 55	20. 50	53,5	16. 50	8. 55
5. 0	20. 45	51,5	16. 55	8. 50
5. 5	20. 40	49,5	17. 0	8. 45
5. 10	20. 35	47,5	17. 5	8. 40
5. 15	20. 30	45,4	17. 10	8. 35
5. 20	20. 25	43,3	17. 15	8. 30
5. 25	20. 20	41,2	17. 20	8. 25
5. 30	20. 15	39,1	17. 25	8. 20
5. 35	20. 10	37,0	17. 30	8. 15
5. 40	20. 5	34,8	17. 35	8. 10
5. 45	20. 0	32,7	17. 40	8. 5
5. 50	19. 55	30,5	17. 45	8. 0
5. 55	19. 50	28,3	17. 50	7. 55
6. 0	19. 45	26,1	17. 55	7. 50
6. 5	19. 40	23,8	18. 0	7. 45
6. 10	19. 35	21,6	18. 5	7. 40
6. 15	19. 30	19,4	18. 10	7. 35
6. 20	19. 25	17,1	18. 15	7. 30
6. 25	19. 20	14,8	18. 20	7. 25
6. 30	19. 15	12,6	18. 25	7. 20
6. 35	19. 10	10,3	18. 30	7. 15
6. 40	19. 5	8,0	18. 35	7. 10
6. 45	19. 0	5,7	18. 40	7. 5
6. 50	18. 55	3,4	18. 45	7. 0
6. 52½	18. 52½	1,1	18. 50	6. 55
		0,0	18. 52½	6. 52½

Right Ascension of the Mid-heaven, the correction of Altitude to be subtracted.

Correction of Observed Altitude.

Right Ascension of the Mid-heaven, the correction of Altitude to be added.

TABLE 2.

RA of MH	10	20	30	40	45	50	55	60	65	70	75	RA of MH
H												H
52 $\frac{1}{2}$,0	,0	,0	,0	,0	,0	,0	,0	,0	,0	,0	52 $\frac{1}{2}$
1. 30	,0	,0	,0	,0	,0	,1	,1	,1	,1	,1	,2	15
2. 0	,0	,0	,1	,1	,1	,2	,2	,2	,3	,4	,6	23. 45
2. 30	,1	,1	,2	,2	,3	,3	,4	,5	,6	,8	,11	23. 15
3. 0	,1	,2	,3	,4	,5	,6	,7	,8	,10	,13	,19	22. 45
3. 30	,1	,2	,4	,6	,7	,8	,10	,12	,15	,19	,26	22. 15
4. 0	,1	,3	,5	,7	,9	,10	,13	,15	,19	,25	,34	21. 45
4. 20	,2	,4	,6	,9	,10	,12	,15	,18	,22	,29	,40	21. 25
4. 40	,2	,4	,7	,10	,11	,14	,16	,20	,25	,32	,45	21. 5
5. 0	,2	,4	,7	,11	,13	,15	,18	,22	,28	,36	,49	20. 45
5. 20	,2	,5	,8	,12	,14	,16	,20	,24	,30	,37	,53	20. 25
5. 40	,3	,5	,9	,12	,15	,17	,21	,26	,32	,40	,56	20. 5
6. 0	,3	,5	,9	,13	,15	,18	,22	,27	,33	,41	,58	19. 45
6. 20	,3	,6	,9	,13	,16	,19	,23	,27	,34	,42	,59	19. 25
6. 40	,3	,6	,9	,13	,16	,19	,23	,28	,34	,42	,60	19. 5
7. 0	,3	,6	,9	,13	,16	,19	,23	,28	,34	,42	,59	18. 45
7. 20	,3	,6	,9	,13	,16	,19	,22	,27	,34	,42	,58	18. 25
7. 40	,3	,6	,9	,13	,15	,18	,22	,26	,32	,40	,56	18. 5
8. 0	,3	,5	,8	,12	,15	,17	,21	,25	,31	,39	,53	17. 45
8. 20	,2	,5	,8	,11	,14	,16	,19	,23	,29	,36	,49	17. 25
8. 40	,2	,5	,7	,10	,13	,15	,18	,22	,27	,34	,45	17. 5
9. 0	,2	,4	,7	,9	,11	,14	,16	,19	,24	,30	,41	16. 45
9. 20	,2	,4	,6	,8	,10	,12	,14	,17	,21	,27	,36	16. 25
9. 40	,2	,3	,5	,7	,9	,10	,12	,15	,18	,22	,31	16. 5
10. 0	,1	,3	,4	,6	,7	,9	,10	,12	,15	,19	,26	15. 45
10. 30	,1	,2	,3	,4	,5	,6	,7	,9	,11	,14	,19	15. 15
11. 5	,1	,1	,2	,3	,3	,4	,5	,5	,7	,8	,11	14. 40
11. 35	,0	,1	,1	,1	,1	,2	,2	,3	,3	,4	,6	14. 10
12. 5	,0	,0	,0	,1	,1	,1	,1	,1	,1	,2	,2	13. 40
12. 52 $\frac{1}{2}$,0	,0	,0	,0	,0	,0	,0	,0	,0	,0	,0	12. 52 $\frac{1}{2}$

RULE.

Enter Table 1. with the Right Ascension of the Mid-heaven in one of the side columns, and in the middle column will be found a Correction to be *added* to, or *subtracted* from, the Observed Altitude (corrected for Refraction,) as directed in the column of Right Ascension. This will give the Latitude near the truth.

Enter Table 2. with the Latitude thus found, at the top, and the Right Ascension of the Mid-heaven at the side; the corresponding Correction *added* to the Latitude as found above, will give the true Latitude.

About the middle of the year 1801, the Right Ascension of the Polar Star will be $52^{\circ} 30'$, and its Declination $88^{\circ} 15' N.$ for that time these Tables are calculated. A correction will therefore be necessary, both before and after that time, to make them accurate; this may be found as follows:

Having found the Polar Star's true place, to correct the error of Right Ascension, *subtract* the quantity above or *add* what it wants, of $52^{\circ} 30'$, from the Right Ascension of the Mid-heaven, before you enter the Tables. To correct the error of Declination, *subtract* it be greater, or *add* if it be less than $88^{\circ} 15' N.$

$\frac{1}{205}$ for every minute, or $\frac{1}{6300}$ for every second, it is greater less than $88^{\circ} 15'$, from the corrections in the Tables be applied to the Altitude.



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